

두 인증서 없는 서명 기법들에 관한 안전성 분석*

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Security Analysis of Two Certificateless Signature Schemes*

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요 약

인증서 없는 공개키 시스템은 기존의 공개키 암호시스템에서 인증서의 필요성을 제거하고 신원 기반 암호시스템에서 키 위탁 문제를 해결하였다. 본 논문에서는 Guo 등과 Wang 등에 의해서 제안된 각각의 인증서 없는 서명 기법들이 공격자 종류 I에 의해 키 대치공격에 취약하다는 것을 보인다. 다시 말해, 서명자의 공개키를 대치할 수 있는 능력을 가진 공격자가 서명자의 비밀키를 알지 못함에도 불구하고 서명을 위조할 수 있음을 보이고 이러한 공격을 방지하기 위한 대응법을 제안한다.

ABSTRACT

Certificateless cryptography eliminates the need of certificates in the public key cryptosystems and solves the inherent key escrow problem in identity-based cryptosystems. This paper demonstrates that two certificateless signature schemes proposed by Guo et al. and Wang et al. respectively are insecure against key replacement attacks by a type I adversary. We show that the adversary who can replace a signer's public key can forge signatures under the replaced public key. We then make a suggestion to prevent the attacks.

Keywords: Certificateless cryptography, Digital signature, Key replacement attack, Forgery

1. Introduction

In 1984, Shamir[11] introduced an identity (ID)-based cryptosystem to simplify key management procedures of the infrastructure (PKI). This notion is to use a binary string which can uniquely identify a user as the user's public key. Examples of such a binary string include email address, IP address and social security number, etc. Certificates are only needed for some trusted authorities called a Private Key

Generator (PKG) which is responsible for generating private keys for users. An inherent problem of the ID-based cryptography is the key escrow problem, i.e., the private key of a user is known to the PKG. The PKG can decrypt any ciphertext and forge signature on any message for any user. In 2003, Al-Riyami and Paterson[1] introduced a certificateless Public Key Cryptosystem (CL-PKC) in order to avoid the inherent key escrow problem of identity-based cryptosystems and not to require certificates to guarantee the authenticity of public keys. A user's private key in a CL-PKC is not generated by the Key Generation Center (KGC) alone. Instead, it is a combination of some contribution of the KGC and some user's chosen secret, in such a way that

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the key escrow problem can be solved. Some additional user's public-key needs to be certified by any trusted authority and CL-PKC schemes are not purely ID-based. Al-Riyami and Paterson proposed a certificateless public-key signature (CLS) but they didn't formalize a security model for unforgeability. However, their CLS scheme was recently found vulnerable to a key replacement attack by Huang et al.[8]. Since Al-Riyami and Paterson's CLS scheme, several CLS schemes have been proposed[4,5,9]. They provided only informal analysis and were subsequently found to be vulnerable to key replacement attacks by type I adversaries[2]. Later, proven secure CLS schemes in the random oracle model[3,8,14] have been proposed. Recently, Liu et al.[10] proposed a provably secure CLS scheme in the standard model. In addition to these direct constructions, there exist a generic construction that converts existing signature schemes in different infrastructures into CLS schemes. Yum and Lee[13] proposed a generic construction for CLS schemes by combining any standard signature (SS) scheme with any ID-based signature (IBS) scheme. Subsequently, Hu et al.[7] showed that this construction is insecure against key replacement attacks and then proposed its improved version by modifying the input of signing algorithm. In particular Hu et al.[7] established a simplified definition and formal security model for CLS schemes which are shown to be more versatile than the previous ones[8]. Recently, Au et al.[2] suggested a malicious-but-passive KGC attack where a KGC may not generate master public/secret key pair honestly to mount the attack, they then modified Hu et al.'s model for capturing the attack. They also showed that Al-Riyami and Paterson's scheme and its variants [2,7,9] are insecure against the malicious-but-passive KGC attacks and the security of the CLS scheme converted from the modified Yum-Lee's construction is preserved in their new model.

Recently, Guo et al.[6] and Wang et al.[12] proposed new efficient CLS schemes based on Li et al.'s scheme[9]. Guo et al. proved its security against a type I adversary and a type II adversary in the

random oracle model under the q -th Strong Diffie-Hellman assumption and the Computational Diffie-Hellman assumption, respectively, while Wang et al. didn't provide its formal security proof. In this paper, we show that two CLS schemes are insecure against key replacement attacks by a type I adversary.

The remainder of this paper is organized as follows. In Section 2, we review Wang et al.'s and Guo et al.'s CLS schemes. In Section 3, we present key replacement attacks on the schemes. Concluding remarks are given in Section 4.

II. Review of Two CLS Schemes

We first review Wang et al.'s and Guo et al.'s CLS schemes that follow Al-Riyami and Paterson's definition[1].

■ Wang et al.'s CLS Scheme

Setup. Given a security parameter k , the algorithm works as follows :

1. Run a generator to output descriptions of G_1 and G_2 of prime order q and a bilinear pairing $e : G_1 \times G_1 \rightarrow G_2$.
2. Choose an arbitrary generator $P \in G_1$.
3. Choose a random $s \in_{\mathcal{R}} \mathbb{Z}_q^*$, set $P_{pub} = sP$, and compute $g = e(P, P)$, where s is a master secret.
4. Choose cryptographic hash functions $H_1 : \{0, 1\}^* \rightarrow \mathbb{Z}_q^*$ and $H_2 : \{0, 1\}^* \times G_2 \rightarrow \mathbb{Z}_q^*$.
5. The system parameters are

$$params = \langle G_1, G_2, e, q, P, P_{pub}, g, H_1, H_2 \rangle .$$

Partial-Private-Key-Extract. This algorithm takes as input a security parameter k , the system parameters $params$, the master secret s and a user A 's identity ID_A , and returns a partial private key corresponding to ID_A . It adopts the blind technique to remove a confidential and authentic channel between A and the KGC .

1. The user A chooses a value $k \in_{\mathcal{R}} \mathbb{Z}_q^*$, computes

kP and then sends $\langle ID_A, kP \rangle$ to the *KGC*.

2. After receiving the message, the *KGC* checks that A has a claim to a particular online identifier ID_A . If it does, the *KGC* computes

$$D'_{ID_A} = [H_1(ID_A) + s]^{-1}P + s(kP),$$

and then sends it to A through an open channel.

3. On the receipt of D'_{ID_A} , A computes a partial private key D_{ID_A} as

$$D_{ID_A} = D'_{ID_A} - k(sP) = [H_1(ID_A) + s]^{-1}P.$$

Notice that A can verify the correctness of the output of the Partial-Private-Key-Extract algorithm by checking that

$$e(D_{ID_A}, H_1(ID_A)P + P_{pub}) = g.$$

Set-Secret-Value. This algorithm takes as input the system parameters $params$ and an identity ID_A , and returns a secret value x_A corresponding to ID_A for a random $x_A \in_R Z_q^*$.

Set-Private-Key. This algorithm takes as input the system parameters $params$, a partial private key D_{ID_A} and a secret value x_A , and returns a (full) private key SK_{ID_A} as

$$SK_{ID_A} = x_A D_{ID_A} = x_A [H_1(ID_A) + s]^{-1}P.$$

Set-Public-Key. This algorithm takes as input the system parameters $params$, an identity ID_A , a secret value x_A and outputs a public key $PK_{ID_A} = \langle X_A, Y_A \rangle$ corresponding to ID_A , where $X_A = x_A^{-1}P$ and $Y_A = x_A^{-1}P_{pub}$.

Sign. Given a message $m \in \{0,1\}^*$ and a private key SK_{ID_A}

1. Choose $a \in_R Z_q^*$, and compute $r = g^a \in G_2$ and $v = H_2(m \| r) \in Z_q^*$.
2. Compute $U = (a + v) \cdot SK_{ID_A} \in G_1$. Then $\sigma = (U, v)$ is a signature on m for $\{ID_A, \langle X_A, Y_A \rangle\}$.

Verify. To verify a signature $\sigma = (U, v)$ on a

message m for $\{ID_A, \langle X_A, Y_A \rangle\}$,

1. Check whether the equality $e(X_A, P_{pub}) = e(Y_A, P)$ holds or not. If it holds, compute $r = e(U, H_1(ID_A)X_A + Y_A) \cdot g^{-v}$.
2. Check whether the equality $v = H_2(m \| r)$ holds or not. If it holds, accept the signature.

■ Guo et al.'s CLS Scheme

Algorithms in Guo et al.'s scheme except the following three algorithms are the same as those in Wang et al.'s scheme.

Set-Partial-Private-Key. Given a security parameter k , the master secret s and an identity ID_A , output $D_{ID_A} = [H_1(ID_A) + s]^{-1}P$ as a partial-private-key correspond to ID_A .

Set-Private-Key. Given a partial private Key D_{ID_A} , an identity ID_A and a secret value x_A , output $SK_{ID_A} = x_A^{-1}D_{ID_A} = [x_A(H_1(ID_A) + s)]^{-1}P$ as a (full) private key correspond to ID_A .

Set-Public-Key. Given an identity ID_A and a secret value x_A , compute $X_A = x_A P$, $Y_A = x_A P_{pub}$ and set $PK_{ID_A} = \langle X_A, Y_A \rangle$.

The main difference of Wang et al.'s scheme from Guo et al.'s scheme is to use the blind technique for eliminating a secure channel between the signer and the KGC in Partial-Private-key-Extract stage.

III. Key Replacement Attacks on the Two CLS Schemes

Now, we present key replacement attacks on the two CLS schemes described in the previous section. In CLS schemes, there exist two types of adversaries with the following capabilities;

- **Type I** adversary A_I as a third party is not allowed to access to the master secret but A_I may replace user public keys of its choices.
- **Type II** adversary A_{II} as a malicious KGC is allowed to access to the master secret but not replace user public keys.

Now, we show that the two CLS schemes are insecure against key replacement attacks by a type I adversary.

■ Key Replacement Attack on Wang et al.'s Scheme

Suppose that a type I adversary A_I wants to forge a certificateless signature of Wang et al.'s scheme. We assume that A_I has obtained a certificateless signature $\sigma = (U, v)$ on m for $\{ID_A, PK_{ID_A}\}$ where $PK_{ID_A} = \langle X_A, Y_A \rangle$, $U = (a+v) \cdot SK_{ID_A}$ and $v = H_2(m \| r)$. Then A_I can forge $\sigma' = (U', v')$ on the same message m for another public key pair $PK'_{ID_A} = \langle X'_A, Y'_A \rangle$, corresponding to ID_A as follows:

- A_I selects a random $t \in_R Z_q^*$ and computes a new public key pair being replaced as $X'_A = t^{-1}X_A = t^{-1}x_A^{-1}P$ and

$$Y'_A = t^{-1}Y_A = t^{-1}x_A^{-1}P_{pub}.$$

- Next, A_I computes $U' = tU$ and sets $v' = v$. Then $\sigma' = (U', v')$ is a valid signature on m for $\{ID_A, PK'_{ID_A}\}$ since it satisfies the verification equations as follow;

$$\begin{aligned} e(X'_A, P_{pub}) &= e(t^{-1}X_A, sP) = e(t^{-1}sX_A, P) \\ &= e(t^{-1}Y_A, P) = e(Y'_A, P) \end{aligned}$$

and $v = H_2(m \| r')$ since

$$\begin{aligned} r' &= e(U', H_1(ID_A)X'_A + Y'_A) \cdot g^{-v'} \\ &= e(U, H_1(ID_A)X_A + Y_A) \cdot g^{-v} \end{aligned}$$

$$\begin{aligned} \text{i.e., } U' &= tU = t(a+v) \cdot SK_{ID_A} \\ &= (a+v)t \cdot SK_{ID_A} = (a+v) \cdot SK'_{ID_A} \end{aligned}$$

where $SK'_{ID_A} = t \cdot SK_{ID_A}$ and SK'_{ID_A} is a valid private key of ID_A corresponding to the replaced public key $PK'_{ID_A} = \langle X'_A, Y'_A \rangle$.

This result shows that it is insecure against a type I adversary since the adversary can forge a user's certificateless signature under the replaced public key. The same attack can be applied to Li et al.'s[9] and to Guo et al.'s[6] CLS schemes since they use the same signing method as Wang et al.'s one.

IV. Conclusion

We presented the key replacement attacks on Wang et al. and Guo et al.'s CLS schemes. Their weakness against the attacks are due to the lack of binding technique between messages and user public keys being signed. These attacks can be prevented by adding a user public key PK_{ID} together with m to the input of the hash function, i.e., $h = H(m \| r \| PK_{ID})$ as described in [13].

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